

Umocnenie dvojčlena:

$$(a \pm b)^2 = a^2 \pm 2ab + b^2, \quad (a \pm b)^3 = a^3 \pm 3a^2b + 3ab^2 \pm b^3 \dots$$

$$(a + b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{n-1}ab^{n-1} + b^n \quad (\text{binomická veta})$$

$$\text{kombinačné číslo: } \binom{n}{k} = \frac{n!}{(n-k)!k!} = \frac{n(n-1)(n-2)\dots(n-k+1)}{k!},$$

$$n! = n(n-1)(n-2)\dots 3 \cdot 2 \cdot 1$$

$$\text{Pascalov trojuholník: } \begin{array}{cccc} & & \binom{0}{0} & \\ & & \binom{1}{0} & \binom{1}{1} \\ & & \binom{2}{0} & \binom{2}{1} & \binom{2}{2} \\ & & \binom{3}{0} & \binom{3}{1} & \binom{3}{2} & \binom{3}{3} \\ & & & \vdots & & \end{array} \quad \text{resp.} \quad \begin{array}{ccccccc} & & & & 1 & & \\ & & & & 1 & 1 & \\ & & & & 1 & 2 & 1 \\ & & & & 1 & 3 & 3 & 1 \\ & & & & 1 & 4 & 6 & 4 & 1 \\ & & & & 1 & 5 & 10 & 10 & 5 & 1 \\ & & & & & & \vdots & & & \end{array}$$

Niektoré rozklady na súčin:

$$a^2 - b^2 = (a - b)(a + b),$$

$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

$$a^n - b^n = (a - b)(a^{n-1} + a^{n-2}b + \dots + ab^{n-2} + b^{n-1})$$

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

Počítanie s mocninami a odmocninami:

$$a^0 = 1, \quad a^r \cdot a^s = a^{r+s}, \quad (a^r)^s = a^{r \cdot s}, \quad \frac{a^r}{a^s} = a^{r-s}, \quad (ab)^r = a^r \cdot b^r,$$

$$\left(\frac{a}{b}\right)^r = \frac{a^r}{b^r}, \quad \sqrt[n]{a} = a^{\frac{1}{n}}, \quad \sqrt[n]{a^m} = (\sqrt[n]{a})^m = a^{\frac{m}{n}}, \quad \sqrt[n \cdot p]{a^{m \cdot p}} = a^{\frac{m}{n}}$$

Vzťahy pre logaritmy:

$$\log_a x = b \Leftrightarrow x = a^b$$

$$\log_a 1 = 0, \quad \ln e = 1, \quad \log_a a^k = k;$$

$$a^{\log_a b} = b, \quad \log_a a^b = b$$

$$\log_a r + \log_a s = \log_a r \cdot s, \quad \log_a r - \log_a s = \log_a \frac{r}{s}, \quad \log_a r^s = s \cdot \log_a r$$

Niektoré goniometrické vzťahy:

$$\sin^2 x + \cos^2 x = 1,$$

$$\operatorname{tg} x \cdot \operatorname{cotg} x = 1;$$

$$\sin 2x = 2 \sin x \cos x,$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$\sin^2 x = \frac{1 - \cos 2x}{2},$$

$$\cos^2 x = \frac{1 + \cos 2x}{2}$$

$$\sin(x \pm y) = \sin x \cos y \pm \sin y \cos x,$$

$$\cos(x \pm y) = \cos x \cos y \mp \sin x \sin y;$$

$$\sin x \pm \sin y = 2 \sin \frac{x \pm y}{2} \cos \frac{x \mp y}{2},$$

$$\cos x + \cos y = 2 \cos \frac{x + y}{2} \cos \frac{x - y}{2},$$

$$\cos x - \cos y = -2 \sin \frac{x + y}{2} \sin \frac{x - y}{2}$$

Postupnosti:

$$\text{Aritmetická} : a_n = a_1 + (n-1)d; \quad s_n = \frac{n}{2}(a_1 + a_n)$$

$$\text{Geometrická} : a_n = a_1 q^{n-1}; \quad s_n = a_1 \frac{q^n - 1}{q - 1} \quad (|q| < 1)$$